# Problem A <br> Secret of Chocolate Poles 

## Time Limit: 1 second

Wendy, the master of a chocolate shop, is thinking of displaying poles of chocolate disks in the showcase. She can use three kinds of chocolate disks: white thin disks, dark thin disks, and dark thick disks. The thin disks are 1 cm thick, and the thick disks are $k \mathrm{~cm}$ thick. Disks will be piled in glass cylinders.

Each pole should satisfy the following conditions for her secret mission, which we cannot tell.

- A pole should consist of at least one disk.
- The total thickness of disks in a pole should be less than or equal to $l \mathrm{~cm}$.
- The top disk and the bottom disk of a pole should be dark.
- A disk directly upon a white disk should be dark and vice versa.

As examples, six side views of poles are drawn in Figure A.1. These are the only possible side views she can make when $l=5$ and $k=3$.


Figure A.1. Six chocolate poles corresponding to Sample Input 1

Your task is to count the number of distinct side views she can make for given $l$ and $k$ to help her accomplish her secret mission.

## Input

The input consists of a single test case in the following format.

$$
l k
$$

Here, the maximum possible total thickness of disks in a pole is $l \mathrm{~cm}$, and the thickness of the thick disks is $k \mathrm{~cm}$. $l$ and $k$ are integers satisfying $1 \leq l \leq 100$ and $2 \leq k \leq 10$.

## Output

Output the number of possible distinct patterns.

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 53 | 6 |

## Sample Input 2 Sample Output 2

| 910 | 5 |
| :--- | :--- |

Sample Input $3 \quad$ Sample Output 3

| 1010 | 6 |
| :--- | :--- |

Sample Input 4

Sample Output 4

20586

Sample Input 5

## Sample Output 5

| 1002 | 3626169232670 |
| :--- | :--- |

## Problem B

## Parallel Lines

## Time Limit: 10 seconds

Given an even number of distinct planar points, consider coupling all of the points into pairs. All the possible couplings are to be considered as long as all the given points are coupled to one and only one other point.

When lines are drawn connecting the two points of all the coupled point pairs, some of the drawn lines can be parallel to some others. Your task is to find the maximum number of parallel line pairs considering all the possible couplings of the points.

For the case given in the first sample input with four points, there are three patterns of point couplings as shown in Figure B.1. The numbers of parallel line pairs are 0,0 , and 1, from the left. So the maximum is 1 .




Figure B.1. All three possible couplings for Sample Input 1

For the case given in the second sample input with eight points, the points can be coupled as shown in Figure B.2. With such a point pairing, all four lines are parallel to one another. In other words, the six line pairs $\left(L_{1}, L_{2}\right),\left(L_{1}, L_{3}\right),\left(L_{1}, L_{4}\right),\left(L_{2}, L_{3}\right),\left(L_{2}, L_{4}\right)$ and $\left(L_{3}, L_{4}\right)$ are parallel. So the maximum number of parallel line pairs, in this case, is 6 .

## Input

The input consists of a single test case of the following format.

```
m
x}1\mp@subsup{y}{1}{
\vdots
xm ym
```



Figure B.2. Maximizing the number of parallel line pairs for Sample Input 2

The first line contains an even integer $m$, which is the number of points $(2 \leq m \leq 16)$. Each of the following $m$ lines gives the coordinates of a point. Integers $x_{i}$ and $y_{i}\left(-1000 \leq x_{i} \leq 1000\right.$, $-1000 \leq y_{i} \leq 1000$ ) in the $i$-th line of them give the $x$ - and $y$-coordinates, respectively, of the $i$-th point.

The positions of points are all different, that is, $x_{i} \neq x_{j}$ or $y_{i} \neq y_{j}$ holds for all $i \neq j$. Furthermore, No three points lie on a single line.

## Output

Output the maximum possible number of parallel line pairs stated above, in one line.

## Sample Input $1 \quad$ Sample Output 1

| 4 |  | 1 |
| :--- | :--- | :--- |
| 0 | 0 |  |
| 1 | 1 |  |
| 0 | 2 |  |
| 2 | 4 |  |


| 8 | 6 |  |
| :--- | :--- | :--- |
| 0 | 0 |  |
| 0 | 5 |  |
| 2 | 2 |  |
| 2 | 7 |  |
| 3 | -2 |  |
| 5 | 0 |  |
| 4 | -2 |  |
| 8 | 2 |  |

## Sample Input 3

Sample Output 3

| 6 |  | 3 |
| :--- | :--- | :--- |
| 0 | 0 |  |
| 0 | 5 |  |
| 3 | -2 |  |
| 3 | 5 |  |
| 5 | 0 |  |
| 5 | 7 |  |

Sample Input 4
Sample Output 4

```
2
-1000 1000
1000-1000
```

Sample Input 5
Sample Output 5

```
16
327449
-509761
-553 515
360 948
147 }87
-694 468
241 320
463 -753
-206 -991
473 -738
-156 -916
-215 54
-112 -476
-452 780
-18 -335
-146 77
```

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## Problem C <br> Medical Checkup

## Time Limit: 2 seconds

Students of the university have to go for a medical checkup, consisting of lots of checkup items, numbered $1,2,3$, and so on.

Students are now forming a long queue, waiting for the checkup to start. Students are also numbered $1,2,3$, and so on, from the top of the queue. They have to undergo checkup items in the order of the item numbers, not skipping any of them nor changing the order. The order of students should not be changed either.

Multiple checkup items can be carried out in parallel, but each item can be carried out for only one student at a time. Students have to wait in queues of their next checkup items until all the others before them finish.

Each of the students is associated with an integer value called health condition. For a student with the health condition $h$, it takes $h$ minutes to finish each of the checkup items. You may assume that no interval is needed between two students on the same checkup item or two checkup items for a single student.

Your task is to find the items students are being checked up or waiting for at a specified time $t$.

## Input

The input consists of a single test case in the following format.

$$
\begin{aligned}
& n t \\
& h_{1} \\
& \vdots \\
& h_{n}
\end{aligned}
$$

$n$ and $t$ are integers. $n$ is the number of the students $\left(1 \leq n \leq 10^{5}\right)$. $t$ specifies the time of our concern $\left(0 \leq t \leq 10^{9}\right)$. For each $i$, the integer $h_{i}$ is the health condition of student $i$ $\left(1 \leq h_{i} \leq 10^{9}\right)$.

## Output

Output $n$ lines each containing a single integer. The $i$-th line should contain the checkup item number of the item which the student $i$ is being checked up or is waiting for, at $(t+0.5)$ minutes after the checkup starts. You may assume that all the students are yet to finish some of the checkup items at that moment.

Sample Input 1
Sample Output 1

| 320 | 5 |
| :--- | :--- |
| 5 |  |
| 7 | 2 |
| 3 | 2 |

Sample Input 2
Sample Output 2
51000000000
180083
5553
2186
3472
2605 180083
180082

1790
180082

# Problem D <br> Making Perimeter of the Convex Hull Shortest 

## Time Limit: 10 seconds

The convex hull of a set of three or more planar points is, when not all of them are on one line, the convex polygon with the smallest area that has all the points of the set on its boundary or in its inside. Your task is, given positions of the points of a set, to find how much shorter the perimeter of the convex hull can be made by excluding two points from the set.

The figures below correspond to the three cases given as Sample Input 1 to 3. Encircled points are excluded to make the shortest convex hull depicted as thick dashed lines.


## Input

The input consists of a single test case in the following format.

```
n
x ( y 
\vdots
xn yn
```

Here, $n$ is the number of points in the set satisfying $5 \leq n \leq 10^{5}$. For each $i,\left(x_{i}, y_{i}\right)$ gives the coordinates of the position of the $i$-th point in the set. $x_{i}$ and $y_{i}$ are integers between $-10^{6}$ and $10^{6}$, inclusive. All the points in the set are distinct, that is, $x_{j} \neq x_{k}$ or $y_{j} \neq y_{k}$ holds when $j \neq k$. It is guaranteed that no single line goes through $n-2$ or more points in the set.

## Output

Output the difference of the perimeter of the convex hull of the original set and the shortest of the perimeters of the convex hulls of the subsets with two points excluded from the original set. The output should not have an error greater than $10^{-4}$.

Sample Input $1 \quad$ Sample Output 1

| 10 | 72.96316928 |
| :--- | :--- |
| -53 | 62 |
| -19 | 58 |
| -11 | 11 |
| -9 | -22 |
| 45 | -7 |
| 37 | -39 |
| 47 | -58 |
| -2 | 41 |
| -37 | 10 |
| 13 | 42 |$\quad$.

## Sample Input 2

Sample Output 2

| 10 | 62.62947992 |
| :--- | :--- |
| -53 | 62 |
| -19 | 58 |
| -11 | 11 |
| -9 | -22 |
| 45 | -7 |
| 43 | -47 |
| 47 | -58 |
| -241 |  |
| -37 | 10 |
| 13 | 42 |$\quad$.

## Sample Input 3

## Sample Output 3

| 10 |  |
| :--- | :--- | :--- |
| -53 | 62 |
| -35 | 47 |
| -11 | 11 |
| -9 | -22 |
| 45 | -7 |
| 43 | -47 |
| 47 | -58 |
| -2 | 41 |
| -37 | 10 |
| 13 | 42 |

61.58166534
$-5362$
-35 47
-11 11
-9 -22
45-7
43-47
47-58
-2 41
1342

## Problem E Black or White

## Time Limit: 2 seconds

Here lies a row of a number of bricks each painted either black or white. With a single stroke of your brush, you can overpaint a part of the row of bricks at once with either black or white paint. Using white paint, all the black bricks in the painted part become white while originally white bricks remain white; with black paint, white bricks become black and black ones remain black. The number of bricks painted in one stroke, however, is limited because your brush cannot hold too much paint at a time. For each brush stroke, you can paint any part of the row with any number of bricks up to the limit.

In the first case of the sample input, the initial colors of four bricks are black, white, white, and black. You can repaint them to white, black, black, and white with two strokes: the first stroke paints all four bricks white and the second stroke paints two bricks in the middle black.

Your task is to calculate the minimum number of brush strokes needed to change the brick colors as specified. Never mind the cost of the paints.

## Input

The input consists of a single test case formatted as follows.

```
nk
s
t
```

The first line contains two integers $n$ and $k(1 \leq k \leq n \leq 500000)$. $n$ is the number of bricks in the row and $k$ is the maximum number of bricks painted in a single stroke. The second line contains a string $s$ of $n$ characters, which indicates the initial colors of the bricks. The third line contains another string $t$ of $n$ characters, which indicates the desired colors of the bricks. All the characters in both $s$ and $t$ are either B or W meaning black and white, respectively.

## Output

Output the minimum number of brush strokes required to repaint the bricks into the desired colors.

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 44 | 2 |
| BWWB |  |
| WBBW |  |


| 43 |
| :--- | :--- |
| BWWB |
| WBBW |

Sample Input $3 \quad$ Sample Output 3

| 43 | 0 |
| :--- | :--- |
| BWWW <br> BWWW |  |

Sample Input 4
Sample Output 4
71
BBWBWBW WBBWWBB

# Problem F <br> Pizza Delivery 

## Time Limit: 2 seconds

Alyssa is a college student, living in New Tsukuba City. All the streets in the city are oneway. A new social experiment starting tomorrow is on alternative traffic regulation reversing the one-way directions of street sections. Reversals will be on one single street section between two adjacent intersections for each day; the directions of all the other sections will not change, and the reversal will be canceled on the next day.

Alyssa orders a piece of pizza everyday from the same pizzeria. The pizza is delivered along the shortest route from the intersection with the pizzeria to the intersection with Alyssa's house.

Altering the traffic regulation may change the shortest route. Please tell Alyssa how the social experiment will affect the pizza delivery route.

## Input

The input consists of a single test case in the following format.

$$
\begin{aligned}
& n m \\
& a_{1} b_{1} c_{1} \\
& \vdots \\
& a_{m} b_{m} c_{m}
\end{aligned}
$$

The first line contains two integers, $n$, the number of intersections, and $m$, the number of street sections in New Tsukuba City ( $2 \leq n \leq 100000,1 \leq m \leq 100000$ ). The intersections are numbered 1 through $n$ and the street sections are numbered 1 through $m$.

The following $m$ lines contain the information about the street sections, each with three integers $a_{i}, b_{i}$, and $c_{i}\left(1 \leq a_{i} \leq n, 1 \leq b_{i} \leq n, a_{i} \neq b_{i}, 1 \leq c_{i} \leq 100000\right)$. They mean that the street section numbered $i$ connects two intersections with the one-way direction from $a_{i}$ to $b_{i}$, which will be reversed on the $i$-th day. The street section has the length of $c_{i}$. Note that there may be more than one street section connecting the same pair of intersections.

The pizzeria is on the intersection 1 and Alyssa's house is on the intersection 2. It is guaranteed that at least one route exists from the pizzeria to Alyssa's before the social experiment starts.

## Output

The output should contain $m$ lines. The $i$-th line should be

- HAPPY if the shortest route on the $i$-th day will become shorter,
- SOSO if the length of the shortest route on the $i$-th day will not change, and
- SAD if the shortest route on the $i$-th day will be longer or if there will be no route from the pizzeria to Alyssa's house.

Alyssa doesn't mind whether the delivery bike can go back to the pizzeria or not.

| Sample Input 1 | Sample Output 1 |
| :---: | :---: |
| 45 | SAD |
| 135 | SAD |
| 346 | SAD |
| 427 | SOSO |
| 2118 | HAPPY |
| 2312 |  |

Sample Input 2
Sample Output 2

| 75 | SOSO |
| :---: | :---: |
| 132 | SAD |
| 163 | SOSO |
| 424 | SAD |
| 625 | SOSO |
| 756 |  |

Sample Output 3

| 10 | 14 |  |  |
| :--- | :--- | :--- | :--- |
| 1 | 7 | 9 | SOSO |
| 1 | 8 | 3 | SAD |
| 2 | 8 | 4 | HAPPY |
| 2 | 6 | 11 |  |
| 3 | 7 | 8 | SOSO |
| 3 | 4 | 4 | SOSO |
| 3 | 2 | 1 |  |
| 3 | 2 | 7 |  |
| 4 | 8 | 4 | SOSO |
| 5 | 6 | 11 |  |
| 5 | 8 | 12 |  |
| 6 | 10 | 6 |  |
| 7 | 10 | 8 |  |
| 8 | 3 | 6 | SAD |

## Problem G

## Rendezvous on a Tetrahedron

## Time Limit: 1 second

One day, you found two worms $P$ and $Q$ crawling on the surface of a regular tetrahedron with four vertices $A, B, C$, and $D$. Both worms started from the vertex $A$, went straight ahead, and stopped crawling after a while.

When a worm reached one of the edges of the tetrahedron, it moved on to the adjacent face and kept going without changing the angle to the crossed edge (Figure G.1).

Write a program which tells whether or not $P$ and $Q$ were on the same face of the tetrahedron when they stopped crawling.

You may assume that each of the worms is a point without length, area, or volume.


Figure G.1. Crossing an edge

Incidentally, lengths of the two trails the worms left on the tetrahedron were exact integral multiples of the unit length. Here, the unit length is the edge length of the tetrahedron. Each trail is more than 0.001 unit distant from any vertices, except for its start point and its neighborhood. This means that worms have crossed at least one edge. Both worms stopped at positions more than 0.001 unit distant from any of the edges.

The initial crawling direction of a worm is specified by two items: the edge $X Y$ which is the first edge the worm encountered after its start, and the angle $d$ between the edge $A X$ and the
direction of the worm, in degrees.


Figure G.2. Trails of the worms corresponding to Sample Input 1

Figure G. 2 shows the case of Sample Input 1. In this case, $P$ went over the edge $C D$ and stopped on the face opposite to the vertex $A$, while $Q$ went over the edge $D B$ and also stopped on the same face.

## Input

The input consists of a single test case, formatted as follows.

$$
\begin{array}{ccc}
X_{P} Y_{P} & d_{P} & l_{P} \\
X_{Q} Y_{Q} & d_{Q} & l_{Q}
\end{array}
$$

$X_{W} Y_{W}(W=P, Q)$ is the first edge the worm $W$ crossed after its start. $X_{W} Y_{W}$ is one of BC, CD or DB.

An integer $d_{W}\left(1 \leq d_{W} \leq 59\right)$ is the angle in degrees between edge $A X_{W}$ and the initial direction of the worm $W$ on the face $\triangle A X_{W} Y_{W}$.

An integer $l_{W}\left(1 \leq l_{W} \leq 20\right)$ is the length of the trail of worm $W$ left on the surface, in unit lengths.

## Output

Output YES when and only when the two worms stopped on the same face of the tetrahedron. Otherwise, output NO.
Sample Input $1 \quad$ Sample Output 1

| CD 301 |  |
| :--- | :--- |
| DB 301 | YES |

## Sample Input 2 <br> Sample Output 2

| BC | 1 | 1 |
| :--- | :--- | :--- |
| DB | 59 | 1 |$\quad$ YES

DB 591

Sample Input 3
Sample Output 3
$\begin{array}{lll}\text { BC } & 29 & 20 \\ \text { BC } & 32 & 20\end{array}$
no

## Problem H

## Homework

## Time Limit: 2 seconds

Taro is a student of Ibaraki College of Prominent Computing. In this semester, he takes two courses, mathematics and informatics. After each class, the teacher may assign homework. Taro may be given multiple assignments in a single class, and each assignment may have a different deadline. Each assignment has a unique ID number.

Everyday after school, Taro completes at most one assignment as follows. First, he decides which course's homework to do at random by flipping a coin. Let $S$ be the set of all the unfinished assignments of the chosen course whose deadline has not yet passed. If $S$ is empty, he plays a video game without doing any homework on that day even if there are unfinished assignments of the other course. Otherwise, with $T \subseteq S$ being the set of assignments with the nearest deadline among $S$, he completes the one with the smallest assignment ID among $T$.

The number of assignments Taro will complete until the end of the semester depends on the result of coin flips. Given the schedule of homework assignments, your task is to compute the maximum and the minimum numbers of assignments Taro will complete.

## Input

The input consists of a single test case in the following format.

$$
\begin{aligned}
& n m \\
& s_{1} t_{1} \\
& \vdots \\
& s_{n} t_{n}
\end{aligned}
$$

The first line contains two integers $n$ and $m$ satisfying $1 \leq m<n \leq 400$. $n$ denotes the total number of assignments in this semester, and $m$ denotes the number of assignments of the mathematics course (so the number of assignments of the informatics course is $n-m$ ). Each assignment has a unique ID from 1 to $n$; assignments with IDs 1 through $m$ are those of the mathematics course, and the rest are of the informatics course. The next $n$ lines show the schedule of assignments. The $i$-th line of them contains two integers $s_{i}$ and $t_{i}$ satisfying $1 \leq s_{i} \leq t_{i} \leq 400$, which means that the assignment of ID $i$ is given to Taro on the $s_{i}$-th day of the semester, and its deadline is the end of the $t_{i}$-th day.

## Output

In the first line, print the maximum number of assignments Taro will complete. In the second line, print the minimum number of assignments Taro will complete.

Sample Input 1
Sample Output 1

| 6 | 3 | 6 |
| :--- | :--- | :--- |
| 1 | 2 | 2 |
| 1 | 5 |  |
| 2 | 3 |  |
| 2 | 6 |  |
| 4 | 5 |  |
| 4 | 6 |  |

Sample Input 2
Sample Output 2

| 6 | 3 | 4 |
| :--- | :--- | :--- |
| 1 | 1 | 3 |
| 2 | 3 |  |
| 4 | 4 |  |
| 1 | 1 |  |
| 2 | 4 |  |
| 3 | 3 |  |

## Problem I

## Starting a Scenic Railroad Service

## Time Limit: 2 seconds

Jim, working for a railroad company, is responsible for planning a new tourist train service. He is sure that the train route along a scenic valley will arise a big boom, but not quite sure how big the boom will be.

A market survey was ordered and Jim has just received an estimated list of passengers' travel sections. Based on the list, he'd like to estimate the minimum number of train seats that meets the demand.

Providing as many seats as all of the passengers may cost unreasonably high. Assigning the same seat to more than one passenger without overlapping travel sections may lead to a great cost cutback.

Two different policies are considered on seat assignments. As the views from the train windows depend on the seat positions, it would be better if passengers can choose a seat. One possible policy (named 'policy-1') is to allow the passengers to choose an arbitrary seat among all the remaining seats when they make their reservations. As the order of reservations is unknown, all the possible orders must be considered on counting the required number of seats.

The other policy (named 'policy-2') does not allow the passengers to choose their seats; the seat assignments are decided by the railroad operator, not by the passengers, after all the reservations are completed. This policy may reduce the number of the required seats considerably.

Your task is to let Jim know how different these two policies are by providing him a program that computes the numbers of seats required under the two seat reservation policies.

Let us consider a case where there are four stations, S1, S2, S3, and S4, and four expected passengers $p_{1}, p_{2}, p_{3}$, and $p_{4}$ with the travel list below.

| passenger | from | to |
| :---: | :---: | :---: |
| $p_{1}$ | S 1 | S 2 |
| $p_{2}$ | S 2 | S 3 |
| $p_{3}$ | S 1 | S 3 |
| $p_{4}$ | S 3 | S 4 |

The travel sections of $p_{1}$ and $p_{2}$ do not overlap, that of $p_{3}$ overlaps those of $p_{1}$ and $p_{2}$, and that of $p_{4}$ does not overlap those of any others.

Let's check if two seats would suffice under the policy-1. If $p_{1}$ books a seat first, either of the two seats can be chosen. If $p_{2}$ books second, as the travel section does not overlap that of $p_{1}$,
the same seat can be booked, but the other seat may look more attractive to $p_{2}$. If $p_{2}$ reserves a seat different from that of $p_{1}$, there will remain no available seats for $p_{3}$ between S1 and S3 (Figure I.1).


Figure I.1. With two seats
With three seats, $p_{3}$ can find a seat with any seat reservation combinations by $p_{1}$ and $p_{2} . p_{4}$ can also book a seat for there are no other passengers between S3 and S4 (Figure I.2).


Figure I.2. With three seats
For this travel list, only three seats suffice considering all the possible reservation orders and seat preferences under the policy-1.

On the other hand, deciding the seat assignments after all the reservations are completed enables a tight assignment with only two seats under the policy-2 (Figure I.3).


Figure I.3. Tight assignment to two seats

## Input

The input consists of a single test case of the following format.

$$
\begin{aligned}
& n \\
& a_{1} b_{1} \\
& \vdots \\
& a_{n} b_{n}
\end{aligned}
$$

Here, the first line has an integer $n$, the number of the passengers in the estimated list of passengers' travel sections ( $1 \leq n \leq 200000$ ). The stations are numbered starting from 1 in their order along the route. Each of the following $n$ lines describes the travel for each passenger by two integers, the boarding and the alighting station numbers, $a_{i}$ and $b_{i}$, respectively $\left(1 \leq a_{i}<b_{i} \leq 100000\right)$. Note that more than one passenger in the list may have the same boarding and alighting stations.

## Output

Two integers $s_{1}$ and $s_{2}$ should be output in a line in this order, separated by a space. $s_{1}$ and $s_{2}$ are the numbers of seats required under the policy- 1 and -2 , respectively.

\left.| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 4 | 22 |
| 1 | 3 |
| 1 | 3 |
| 3 | 6 |
| 3 | 6 |$\right)$


| Sample Input 2 | Sample Output 2 |
| :--- | :--- |
| 4 | 32 |
| 1 | 2 |
| 2 | 3 |
| 1 | 3 |
| 3 | 4 |

## Sample Input 3 <br> Sample Output 3

| 10 | 6 |
| :--- | :--- |
| 84302 | 5 |
| 275327 |  |
| 364538 |  |
| 26364 |  |
| 29386 |  |
| 545955 |  |
| 715965 |  |
| 404415 |  |
| 903942 |  |
| 150402 |  |

## Problem J String Puzzle <br> Time Limit: 2 seconds

Amazing Coding Magazine is popular among young programmers for its puzzle solving contests offering catchy digital gadgets as the prizes. The magazine for programmers naturally encourages the readers to solve the puzzles by writing programs. Let's give it a try!

The puzzle in the latest issue is on deciding some of the letters in a string (the secret string, in what follows) based on a variety of hints. The figure below depicts an example of the given hints.


The first hint is the number of letters in the secret string. In the example of the figure above, it is nine, and the nine boxes correspond to nine letters. The letter positions (boxes) are numbered starting from 1, from the left to the right.

The hints of the next kind simply tell the letters in the secret string at some specific positions. In the example, the hints tell that the letters in the 3rd, 4th, 7th, and 9th boxes are C, I, C, and $P$, respectively.

The hints of the final kind are on duplicated substrings in the secret string. The bar immediately below the boxes in the figure is partitioned into some sections corresponding to substrings of the secret string. Each of the sections may be connected by a line running to the left with another bar also showing an extent of a substring. Each of the connected pairs indicates that substrings of the two extents are identical. One of this kind of hints in the example tells that the letters in boxes 8 and 9 are identical to those in boxes 4 and 5, respectively. From this, you can easily deduce that the substring is IP.

Note that, not necessarily all of the identical substring pairs in the secret string are given in the hints; some identical substring pairs may not be mentioned.

Note also that two extents of a pair may overlap each other. In the example, the two-letter substring in boxes 2 and 3 is told to be identical to one in boxes 1 and 2 , and these two extents share the box 2 .

In this example, you can decide letters at all the positions of the secret string, which are "CCCIPCCIP". In general, the hints may not be enough to decide all the letters in the secret string.

The answer of the puzzle should be letters at the specified positions of the secret string. When the letter at the position specified cannot be decided with the given hints, the symbol ? should be answered.

## Input

The input consists of a single test case in the following format.

| $n$ | $a b$ | $q$ |
| :--- | :--- | :--- |
| $x_{1}$ | $c_{1}$ |  |
| $\vdots$ |  |  |
| $x_{a}$ | $c_{a}$ |  |
| $y_{1}$ | $h_{1}$ |  |
| $\vdots$ |  |  |
| $y_{b}$ | $h_{b}$ |  |
| $z_{1}$ |  |  |
| $\vdots$ |  |  |
| $z_{q}$ |  |  |

The first line contains four integers $n, a, b$, and $q$. $n\left(1 \leq n \leq 10^{9}\right)$ is the length of the secret string, $a(0 \leq a \leq 1000)$ is the number of the hints on letters in specified positions, $b$ $(0 \leq b \leq 1000)$ is the number of the hints on duplicated substrings, and $q(1 \leq q \leq 1000)$ is the number of positions asked.

The $i$-th line of the following $a$ lines contains an integer $x_{i}$ and an uppercase letter $c_{i}$ meaning that the letter at the position $x_{i}$ of the secret string is $c_{i}$. These hints are ordered in their positions, i.e., $1 \leq x_{1}<\cdots<x_{a} \leq n$.

The $i$-th line of the following $b$ lines contains two integers, $y_{i}$ and $h_{i}$. It is guaranteed that they satisfy $2 \leq y_{1}<\cdots<y_{b} \leq n$ and $0 \leq h_{i}<y_{i}$. When $h_{i}$ is not 0 , the substring of the secret string starting from the position $y_{i}$ with the length $y_{i+1}-y_{i}$ (or $n+1-y_{i}$ when $i=b$ ) is identical to the substring with the same length starting from the position $h_{i}$. Lines with $h_{i}=0$ does not tell any hints except that $y_{i}$ in the line indicates the end of the substring specified in the line immediately above.

Each of the following $q$ lines has an integer $z_{i}\left(1 \leq z_{i} \leq n\right)$, specifying the position of the letter in the secret string to output.

It is ensured that there exists at least one secret string that matches all the given information. In other words, the given hints have no contradiction.

## Output

The output should be a single line consisting only of $q$ characters. The character at position $i$ of the output should be the letter at position $z_{i}$ of the the secret string if it is uniquely determined from the hints, or ? otherwise.

Sample Input 1
Sample Output 1

| 9 | 4 | 5 | 4 |
| :--- | :--- | :--- | :--- |
| 3 | C | ICPC |  |
| 4 | I |  |  |
| 7 | C |  |  |
| 9 | P |  |  |
| 2 | 1 |  |  |
| 4 | 0 |  |  |
| 6 | 2 |  |  |
| 7 | 0 |  |  |
| 8 | 4 |  |  |
| 8 |  |  |  |
| 1 |  |  |  |
| 9 |  |  |  |
| 6 |  |  |  |

## Sample Input 2 Sample Output 2

```
1000000000 1 1 2
?A
20171217 A
3 1
42
987654321
```


## Problem K Counting Cycles

## Time Limit: 4 seconds

Given an undirected graph, count the number of simple cycles in the graph. Here, a simple cycle is a connected subgraph all of whose vertices have degree exactly two.

## Input

The input consists of a single test case of the following format.

$$
\begin{aligned}
& n \\
& u_{1} \\
& u_{1} \\
& \vdots \\
& u_{m}
\end{aligned} v_{m}
$$

A test case represents an undirected graph $G$.
The first line shows the number of vertices $n(3 \leq n \leq 100000)$ and the number of edges $m$ $(n-1 \leq m \leq n+15)$. The vertices of the graph are numbered from 1 to $n$.

The edges of the graph are specified in the following $m$ lines. Two integers $u_{i}$ and $v_{i}$ in the $i$-th line of these $m$ lines mean that there is an edge between vertices $u_{i}$ and $v_{i}$. Here, you can assume that $u_{i}<v_{i}$ and thus there are no self loops.

For all pairs of $i$ and $j(i \neq j)$, either $u_{i} \neq u_{j}$ or $v_{i} \neq v_{j}$ holds. In other words, there are no parallel edges.

You can assume that $G$ is connected.

## Output

The output should be a line containing a single number that is the number of simple cycles in the graph.

\left.| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 4 | 5 |
| 1 | 2 |
| 1 | 3 |
| 1 | 4 |
| 2 | 3 |
| 3 | 4 |$\right) 3$


| 7 | 9 | 3 |
| :--- | :--- | :--- |
| 1 | 2 |  |
| 1 | 3 |  |
| 2 | 4 |  |
| 2 | 5 |  |
| 3 | 6 |  |
| 3 | 7 |  |
| 2 | 3 |  |
| 4 | 5 |  |
| 6 | 7 |  |

Sample Input 3
Sample Output 3

| 4 | 6 |  |
| :--- | :--- | :--- |
| 1 | 2 |  |
| 1 | 3 |  |
| 1 | 4 |  |
| 2 | 3 |  |
| 2 | 4 |  |
| 3 | 4 |  |

